

# CHAPTER 7: EXPONENTS AND EXPONENTIAL FUNCTIONS



7.1

APPLY EXPONENT  
PROPERTIES  
INVOLVING  
PRODUCTS



# Exponents

- Exponent – the \_\_\_\_\_ the \_\_\_\_\_  
is \_\_\_\_\_
- EX:

# 1) Product of Powers Property

- When you \_\_\_\_\_, \_\_\_\_\_  
the \_\_\_\_\_.
- EX:

# EX:

- Simplify the expression. Write your answer using exponents.
- $(-7)^2(-7)^8$
- $x^2 \cdot x^6 \cdot x$

## 2) Power of a Power Property

- When you \_\_\_\_\_,  
\_\_\_\_\_ the \_\_\_\_\_.
- EX:

# EX:

- Simplify the expression. Write your answer using exponents.
- $(4^2)^7$
- $[(-2)^4]^5$
- $[(m + 1)^6]^3$

# 3) Power of a Product Property

- When a \_\_\_\_\_ is \_\_\_\_\_  
\_\_\_\_\_, raise \_\_\_\_\_ to the  
\_\_\_\_\_.
- EX:



# EX:

- Simplify each expression. Write your answer using exponents.
- $(20 \cdot 17)^3$

# EX: Simplify each expression.

□  $(-4x)^2$

$(2x^3)^2 \cdot x^4$

□  $-(4x)^2$

$$\square (-10x^6)^2 \cdot x^2$$

$$\square (3x^5)^3(2x^7)^2$$

# Order of Magnitude

- The **order of magnitude** of a quantity is the \_\_\_\_\_ that is \_\_\_\_\_ to the \_\_\_\_\_ of the quantity.

- An \_\_\_\_\_

- EX:

- [Order of Magnitude](#)

# EX:

- A box of staples contains  $10^4$  staples. How many staples do  $10^2$  boxes contain?

# EX:

- There are about 1 billion grains of sand in 1 cubic foot of sand. Use order of magnitude to find about how many grains of sand are in 25 million cubic feet of sand.

7.2

APPLY EXPONENT PROPERTIES  
INVOLVING QUOTIENTS

# 1) Quotient of Powers Property

- When \_\_\_\_\_ with  
\_\_\_\_\_, \_\_\_\_\_ the  
\_\_\_\_\_.
- EX:



# EX:

- Simplify the expression. Write your answer using exponents.

- $\frac{(-4)^9}{(-4)^2}$

- $\frac{9^4 \cdot 9^3}{9^2}$

## 2) Power of a Quotient Property

- When a \_\_\_\_\_ is \_\_\_\_\_  
\_\_\_\_\_, raise \_\_\_\_\_ the  
\_\_\_\_\_ and the \_\_\_\_\_ to  
the power and \_\_\_\_\_ if possible.
- EX:

# EX: Simplify the Expression.

□  $(-7/x)^2$

□  $(x^2/4y)^2$

□  $(-5/y)^3$

$$\square (2s/3t)^3 \cdot (t^5/16)$$

$$\square (3x^2/3y^3)^2$$

# EX:

- The order of magnitude of the brightness of the Milky Way is  $10^{36}$  watts. The order of magnitude of the brightness of a gamma ray burster is  $10^{45}$  watts. How many times brighter is the gamma ray burster than the Milky Way?
- [http://www.youtube.com/watch?v=P2ESs1rPO\\_A](http://www.youtube.com/watch?v=P2ESs1rPO_A)



7.3

DEFINE AND USE ZERO AND  
NEGATIVE EXPONENTS

# Zero Power

- Anything raised to the \_\_\_\_\_ is \_\_\_\_\_.
- EX:
- WHY:

# Negative Exponents

- When you have a \_\_\_\_\_ in the \_\_\_\_\_:
  - ▣ Put it in the \_\_\_\_\_ and make it \_\_\_\_\_.
  - ▣ EX:
  
- When you have a \_\_\_\_\_ in the \_\_\_\_\_:
  - ▣ Put it in the \_\_\_\_\_ and make it \_\_\_\_\_.
  - ▣ EX:
  
- NOTE: Negative exponents represent \_\_\_\_\_ numbers.



EX:

Evaluate the expression.

---

- Write your answer using only positive exponents.

EX:

Simplify the expression.

- Write your answer using only positive exponents.

# EX:

- The mass of one peppercorn is about  $10^{-2}$  gram. About how many peppercorns are in a box containing 1 kilogram of peppercorns?

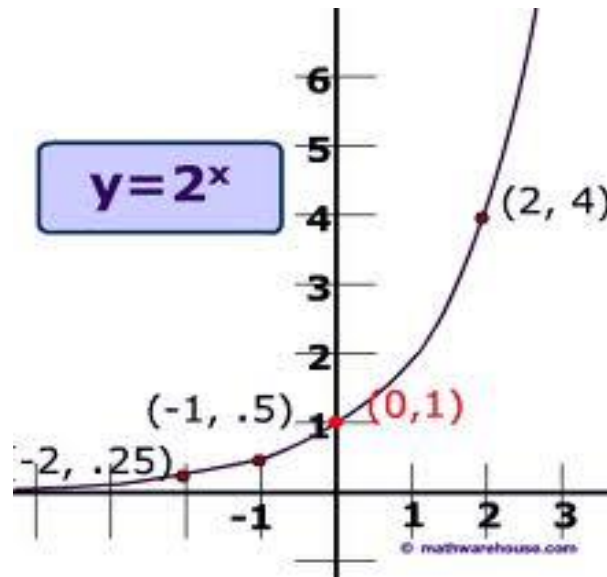


7.4

WRITE AND GRAPH  
EXPONENTIAL GROWTH  
FUNCTIONS

# Exponential Functions

- An **exponential function** is a function in the form of:
  - EX:
- They are \_\_\_\_\_ functions.
  - They have graphs that are \_\_\_\_\_.



# Exponential Function Table

x	-2	-1	0	1	2
y	2	4	8	16	32

# To write a rule for a function table:

- 1) Decide what \_\_\_\_\_ each \_\_\_\_\_ is being \_\_\_\_\_.

  - \_\_\_\_\_.

- 2) Find the \_\_\_\_\_ when \_\_\_\_\_.

  - \_\_\_\_\_.

- 3) Fill in \_\_\_\_\_ into \_\_\_\_\_.

# EX: Write a rule for the function.

x	-2	-1	0	1	2
y	3	9	27	81	243



# EX: Write a rule for the function.

x	-2	-1	0	1	2
y	$\frac{2}{9}$	$\frac{2}{3}$	2	6	18

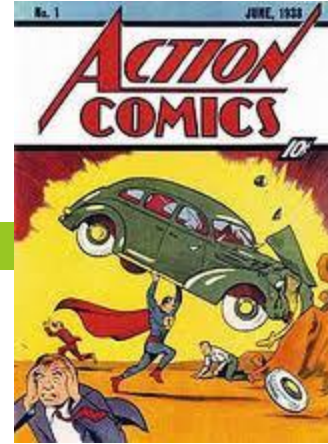
# Exponential Growth

- When a quantity \_\_\_\_\_ by the \_\_\_\_\_ over \_\_\_\_\_.
- EX: Each year the value of an antique car increases by 50%.
  
- Exponential growth is different from linear growth because \_\_\_\_\_ increases by the \_\_\_\_\_ each time interval, \_\_\_\_\_.

# Exponential Growth Model

- 
- $a$  is the \_\_\_\_\_
- $(1 + r)$  is the \_\_\_\_\_
- $r$  is the \_\_\_\_\_
- $t$  is the \_\_\_\_\_

# EX:



- The owner of an original copy of a 1938 comic book sold it at an auction in 2005. The owner bought the comic book for \$55 in 1980. The value of the comic book increased at a rate of 2.8% per year.
  - A) Write a function that models the value of the comic book over time.
  - B) What was the approximate value of the comic book at the time of the auction in 2005? Round your answer to the nearest dollar.



# Compound Interest

- Interest earned on both an \_\_\_\_\_ and on \_\_\_\_\_.
- EX: You put \$125 in a savings account that earns 2% interest compounded yearly. What will the balance in your account be after 5 years?

7.5

WRITE AND GRAPH  
EXPONENTIAL DECAY  
FUNCTIONS

# EX: Write a rule for the function.

x	-1	0	1	2
y	5	1	$1/5$	$1/25$



# Exponential Decay

- When a quantity \_\_\_\_\_ by the \_\_\_\_\_ over \_\_\_\_\_.
- ▣ EX: The number of acres of forests in the U.S. decreases by 0.5% each year.

# Exponential Decay Model

- 
- $a$  is the \_\_\_\_\_
- $(1-r)$  is the \_\_\_\_\_
- $r$  is the \_\_\_\_\_
- $t$  is the \_\_\_\_\_

# EX:

- A farmer bought a tractor in 1999 for \$30,000. The value of the tractor has been decreasing at a rate of 18% per year.
- Write a function that models the value of the tractor over time.
- What was the approximate value of the tractor in 2005?





# Exponential Decay vs. Exponential Growth

Exponential Decay

$$y = ab^x$$
$$b < 1$$

$a$   $(0, a)$



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Exponential Growth

$$y = ab^x$$

$a$   $(0, a)$



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# Graph Examples:

