Chapter 1 Expressions, Equations, and Functions

## Sec 1.1 Evaluate Expressions

#### • Variable

• EX:

• EX:

### • Algebraic Expression – a collection of \_\_\_\_\_, \_\_\_\_, and \_\_\_\_\_without an equal sign.

• Evaluate an Expression – to substitute a number for each variable and

• EX:
• Evaluate the expression.
• 0.6x when x = 4

$$o \frac{24}{y}$$
 when y = 6

$$\frac{2}{3}a$$
 when  $a = \frac{1}{2}$ 

• 
$$b - \frac{1}{2}$$
 when  $b = \frac{5}{6}$ 

## EX: Evaluate the Expression

 You and your friend are going to see a movie. You pay for both admissions. Your total cost (in dollars) can be represented by the expression 2a, where a is the cost of admission. If each admission costs \$7.75, what is your total cost?

#### • **Power** – an expression that represents



• Base – the big, \_\_\_\_\_number

• **Exponent** – the small number that represents\_\_\_\_\_



## EX: Evaluate the expression. • $x^3$ when x = 8

•  $k^2$  when k = 2.5

• d<sup>4</sup> when d = 
$$\frac{1}{2}$$

- Exponents are used in the formulas for area and volume.
- Area of a Square:



#### • Volume of a Cube:



## EX:

Each edge of the storage cube shown is 14 inches long. The storage cube is made so that it can be folded flat when not in use.

- Find the area of the storage cube if it is folded flat.
- Find the volume of the storage cube.





Sec 1.2 Apply Order of Operations

## Order of Operations - the correct order for evaluating/simplifying an expression

### • Order of Operations:

• P\_\_\_\_\_ – simplify expressions inside the parentheses/grouping symbols

- E\_\_\_\_\_ simplify all powers
- M\_\_\_\_and D\_\_\_\_-left to right
- A \_\_\_\_\_ and S \_\_\_\_\_ left to right

#### • **PEMDAS** – "Please Excuse My Dear Aunt Sally"

## EX: Evaluate the expressions.

#### $\circ$ 27 ÷ 3<sup>2</sup> · 2 – 3

**○** 10 + 2·4<sup>2</sup>

#### • $32 \div 2^3 + 6$

## Grouping Symbols

- Parentheses:
- Brackets:
- Fraction Bar:
- Note:
- Always start with the \_\_\_\_\_\_ grouping symbol and work your way out.
- Always follow the \_\_\_\_\_\_ inside each individual grouping symbol.
- For a fraction bar, do what is \_\_\_\_\_\_ and \_\_\_\_\_\_ it before you divide.

## EX: Evaluate each expression. • 4(3 + 9)

**○** 3(8 – 2<sup>2</sup>)

### • 2[(9 + 3) ÷ 4]

# EX: Evaluate each expression when y = 8.

• y<sup>2</sup> - 3



## EX:

You join an online music service. The total cost (in dollars) of downloading 3 singles at \$.99 each and 2 albums at \$9.95 each is given by the expression 3(0.99) + 2(9.95).
Find the total cost.

• You have \$25 to spend. How much will you have left?



Sec 1.3 Write Expressions To translate verbal phrases into mathematical expressions, look for KEY WORDS.

• Key Words

• EX: The sum of 8 and a number x

## Key Words

#### • EX: 7 less than a number y

• NOTE: Order matters!

0

### • Key Words

#### • EX: $\frac{1}{2}$ of a number z

### Key Words

#### • EX: The quotient of 6 and a number a.

• NOTE: Order matters!

0

• NOTE: Anytime you multiply or divide a by something, you must put the sum or difference in

• EX: 3 times the sum of 7 and a number y

## EX: Write an expression for the situation.

• A piece of rope L feet long is cut from a rope 10 feet long. Write an expression for the length of the remaining piece.

## • Each person's share if p people are to divide \$90 evenly.

## EX: Translate the verbal phrase into an expression.

• Three more than half of a number x

• Product of four and a number y

• 4 less than 6 times a number n

## • The difference of 22 and the square of a number m

• The quotient when the quantity 10 plus a number x is divided by 2

- Rate a \_\_\_\_\_\_ that compares two quantities measured in \_\_\_\_\_.
  EX:
- Unit Rate when the \_\_\_\_\_\_
  of the \_\_\_\_\_\_.
  EX:

- Note:
- to turn a rate into a unit rate.
  When comparing unit rates, make sure your units are the \_\_\_\_\_.

# EX: Tell which rate is greater. \$3.50 for 25 ounces, or \$4.75 for 40 ounces

# EX: Find the unit rate in feet per second.

- Note: Multiply by a \_ to convert the units.
- A car travels 150 miles in 3 hours.

### • 600 yards/1 minute

## EX:

• You are ordering Detroit Lions tickets online. Each ticket costs \$55 and there is a \$6 charge no matter how many tickets are ordered. Write an expression for the cost (in dollars) of ordering the tickets. Then find the total cost if you order 8 tickets.



Sec 1.4 Write Equations and Inequalities
## • Equation – a mathematical sentence with an \_\_\_\_\_

• EX:

Inequality – a \_\_\_\_\_\_ of two expressions
EX:

### Symbols:

### Combining Inequalities

• Two \_\_\_\_\_\_ inequalities can be \_\_\_\_\_\_to form one

• EX: x > 8 and x < 15 is the same as:

Read "x is greater than 8 and less than 15"

# EX: Write an equation or inequality.

• The difference of twice a number k and 8 is 12.

• The product of 6 and a number n is at most 24.

## • The sum of y and 1 is no less than 5 and no more than 13.

## • The quotient of a number p and 12 is at least 30.

# EX: Write an equation or inequality and solve.

• Your student senate budget is \$300. You want to buy the members t-shirts for \$6 each. Write an inequality that represents the number of shirts you can buy without going over budget.

Sec 1.5 Use a Problem Solving Plan

### A Problem Solving Plan

- Step 2: Make a \_\_\_\_\_ to Solve. • EX:
- Step 3: \_\_\_\_\_ the Problem. • EX:

#### • Step 4: Check.

• See if your answer is reasonable.

### Formula – a \_\_\_\_

Formulas that should be memorized:
Temperature:





#### • Distance Traveled:



#### • Profit:



#### • Area of a Rectangle:

• | = \_\_\_\_\_

• w = \_\_\_\_\_

#### • Area of a Triangle:

- b = \_\_\_\_\_
- h = \_\_\_\_\_

#### • Perimeter:

### EX: Solve

 One day this summer the temperature in Ontario, Canada was 30 degree Celsius. The temperature in Monroe, MI was 95 degrees Fahrenheit. Which temperature was higher?

# • What is the interest on \$1500 invested for 3 years in an account that earns simple interest at a rate of 5% per year?

## • A bike travels at a rate of 20 mph. How far will it travel in 6 hours?

• A gardener determines the cost of planting daffodil bulbs to be \$2.40 per square foot. How much will it cost to plant daffodil bulbs in a rectangular garden that is 12 feet long and 5 feet wide?





Sec 1.6 Use Precision and Measurement

#### Precision -

- How \_\_\_\_\_\_ a measurement is.
  Precise measurements in general have:
  More \_\_\_\_\_\_
  - Have \_\_\_\_\_\_units
- EX: A watch that measures in seconds is more precise than a watch that measures in minutes, because a second in smaller than a minute.

## • EX: Which side of the ruler would give a more precise measurement?



## EX: Choose the more precise measurement.

• 21.13 oz ; 21.4 oz

• 14 
$$\frac{1}{2}$$
 in. ; 2  $\frac{5}{8}$  in.

• 14 mm ; 2 cm

• 2.5 hr; 90 min

### Significant Digits -

- The digits in a \_\_\_\_\_ that carry meaning.





#### Rules for Determining Sig. Digits

- 1) All \_\_\_\_\_are significant.
  - EX: 114.67 has 5 sig dig
- 2) Zeros that are to the <u>of both</u> the last nonzero digit and the decimal point are significant.
  - EX: 0.0000500 has 3 sig dig
- 3) \_\_\_\_\_between sig digits are significant.
  - EX: 7000.8 has 5 sig dig
- 4) Zeros at the \_\_\_\_\_ of whole numbers are usually assumed to be nonsignificant.
  EX: 300 has 1 sig dig

# EX: Determine the number of sig dig in each measurement.

- 800.20 ft
- 0.0005 cm
- 36,500 yd
- o 67.00 m
- 60 sec

Sec 1.7 Represent Functions as Rules and Tables

#### Function -

• A set of \_\_\_\_\_ (called the \_\_\_\_\_) and \_\_\_\_\_ (called the \_\_\_\_\_) such that each input is paired with

- \_output.
- EX: Pumping Gas the total cost depends on the number of gallons you pumped.
  - So the total cost is a **function** of the number of gallons.

### EX: Birthday Function

- People Domain
- Birthdays Range
- Each person can only have \_\_\_\_\_ birthday.

• But, more than one person can have the

## Functions can be represented as tables.EX:

Input (days)	Output (\$)
1	15
2	20
4	30
6	40
9	55
11	65



# EX: Tell whether the pairing is a function.



# EX: Tell whether the pairing is a function.

	_	_	_	_	_	_
Input						
Output						



#### • A function may also be represented by an

- Variable (x) input values
- Variable (y) output values
  - The value of the dependent variable **depends** on the value of the independent variable.

Rule: The output is 6 less than the input.
Equation:

• Table:

Input, x	10	9	8	7	6
Output, y					

• Make a table for the function  $y = \frac{1}{2}x + 4$ with domain 0, 5, and 10. Then identify the range of the function.

• Write a rule for the function. Then identify the domain and range.

Time (hours)	1	2	3	4
Pay (dollars)	8	16	24	32

• You are buying concert tickets that cost \$15 each. You can buy up to 6 tickets. Write the amount (in dollars) you spend as a function of the number of tickets you buy. Identify the independent and dependent variables. Then identify the domain and range of the function.





Sec 1.8 Represent Functions as Graphs
# Functions

#### Functions can also be represented as \_\_\_\_\_, by putting the values from a

table into



#### • NOTE: (x, y)



### EX:

 Graph the function y = 2x – 1 with the domain 1, 2, 3, 4, and 5 by making a table and then plotting the ordered pairs.

		у 📥				
		6				
		5				
		4				
		β				
		2				
		1				
						x
		<u> </u>			<u> </u>	
-0 -2 -4	4 -3 -2 -	1 0	1 2	3	45	0
-6 -2 -4	4 -3 -2 -	1 -1	1 2	3	4 5	0
-6 -2 -4	4 -3 -2 -	1 • -1 -2	1 2	3	4 5	0
	4 -3 -2 -	1 -1 -2 -3	1 2	3	4 5	0
	4 -3 -2 -	1 -1 -2 -3	1 2	3	4 5	0
	4 -3 -2 -	1 -1 -2 -3 -4 -5	1 2	3	4 5	

## EX:

• Write a rule for the function represented by the graph. Identify the domain and the range of the function.



### EX:

• Graph the function that represent the enrollment at SMCC since 2004. (t = 0 corresponds to 2004)

• Describe what happened to the enrollment as time went on.

Years since 2004, t	0	1	2	3	4	5	6	7	8
Enroll ment , e	398	405	400	410	413	420	427	445	451

Name : \_\_\_\_\_

\_\_\_\_

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