

**CHAPTER 6**  
**SOLVING SYSTEMS OF**  
**EQUATIONS AND**  
**INEQUALITIES**

6.1

**SOLVE LINEAR SYSTEMS  
BY GRAPHING**

# SYSTEMS OF LINEAR EQUATIONS

■ **System of Linear Equations** - \_\_\_\_\_ linear equations to be \_\_\_\_\_ at the \_\_\_\_\_

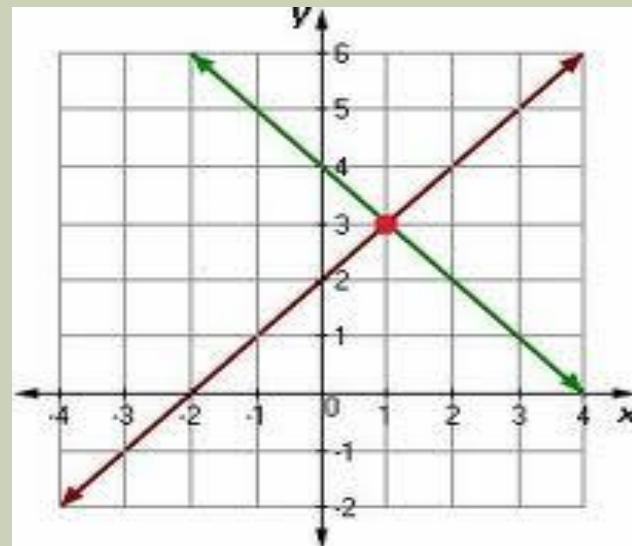
■ EX:

■ **Solution of a System of Linear Equations** - an \_\_\_\_\_ that satisfies \_\_\_\_\_ in the system.

■ EX:

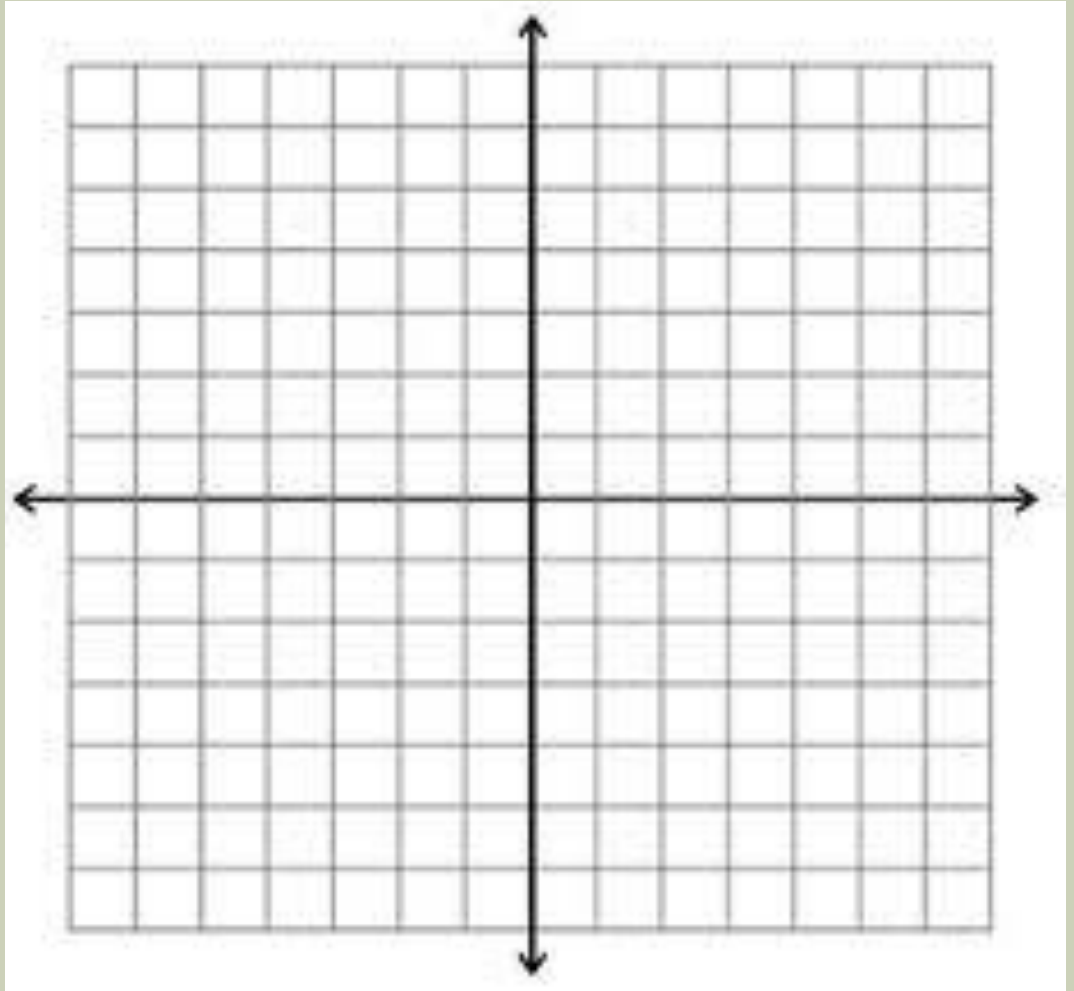
# METHOD 1: SOLVING BY GRAPHING

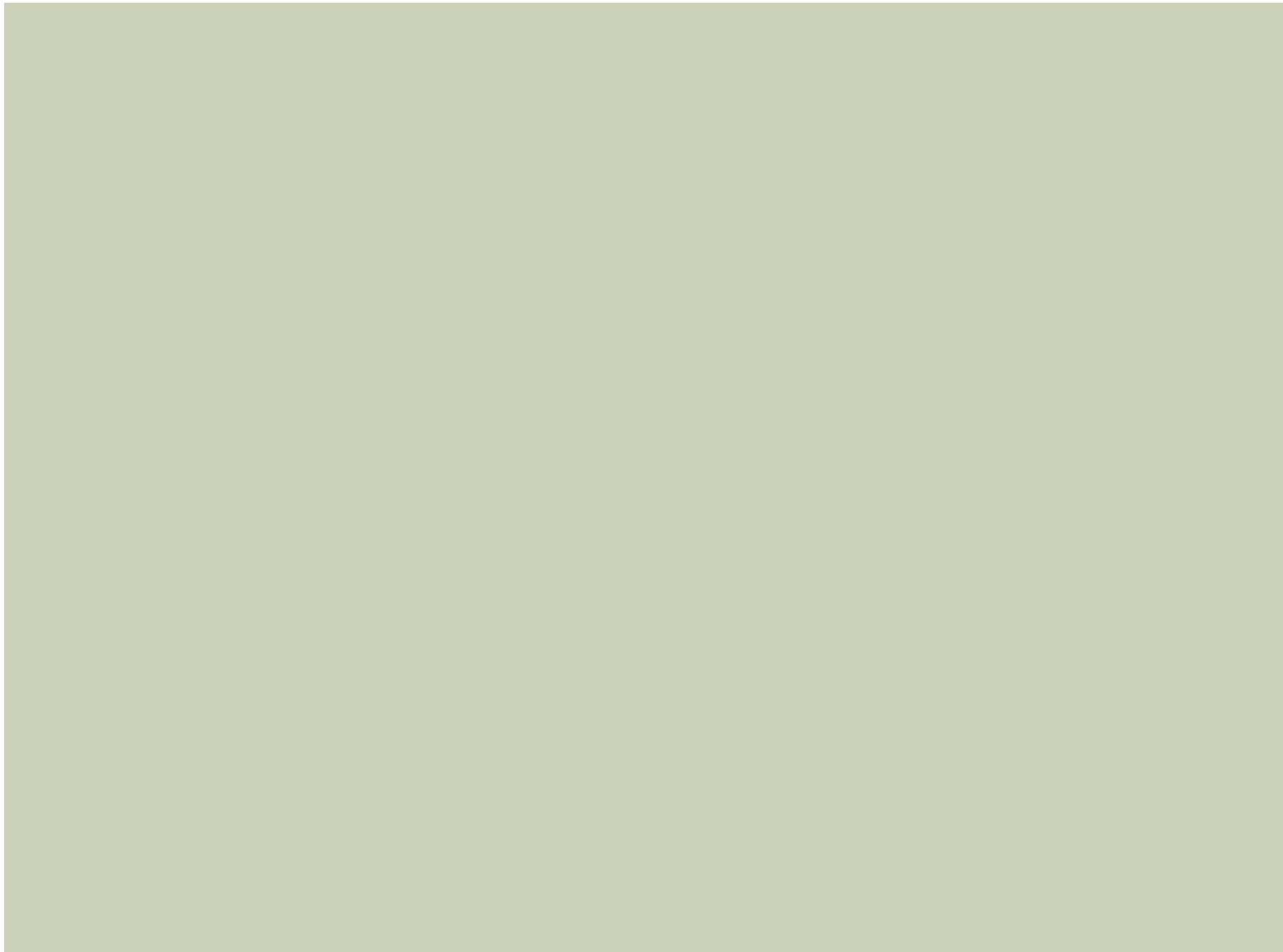
- 1) Graph \_\_\_\_\_ equations in the \_\_\_\_\_  
\_\_\_\_\_  
■ Use \_\_\_\_\_ form.  
■ Use your slope to go up and over \_\_\_\_\_.
  
- 2) The \_\_\_\_\_ where the two lines \_\_\_\_\_  
in the \_\_\_\_\_.



# EX: SOLVE THE LINEAR SYSTEM BY GRAPHING.

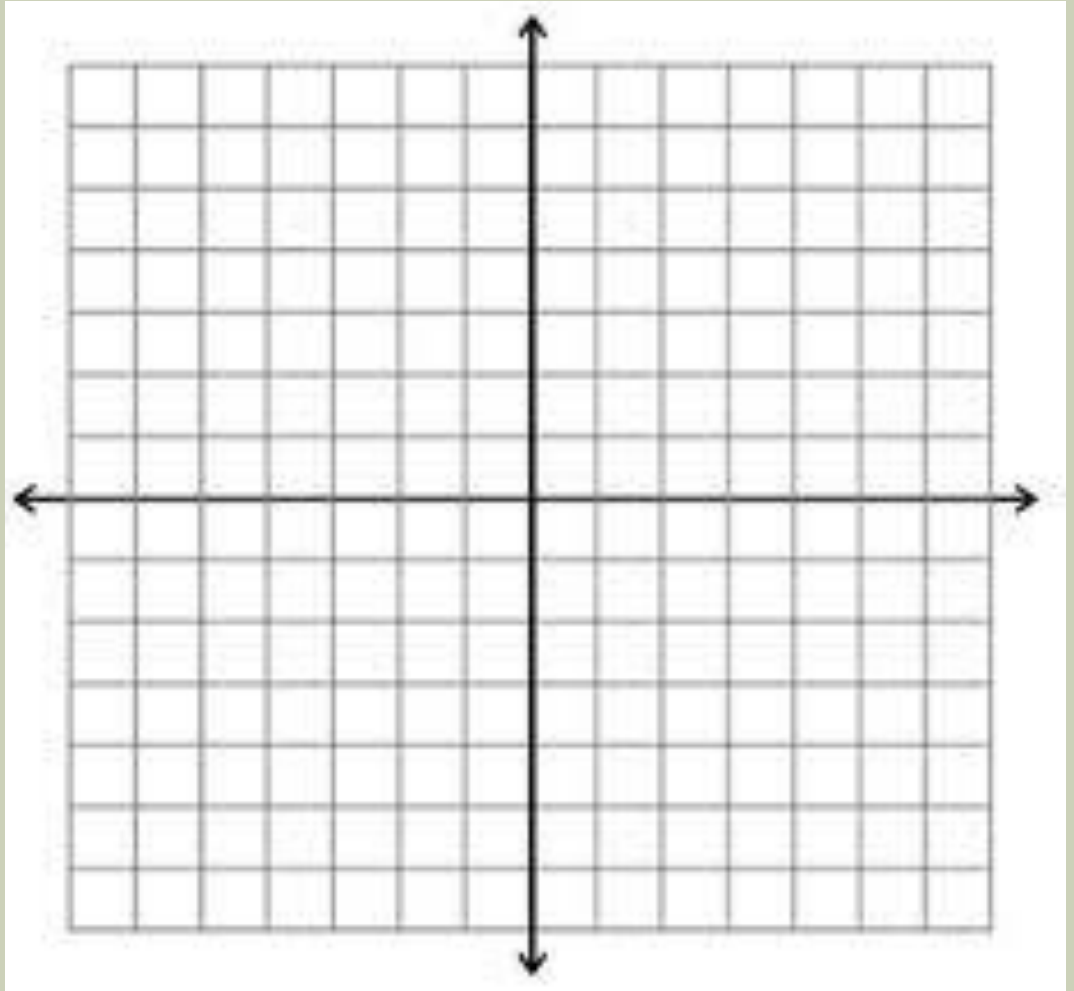
- $x - y = 5$
- $3x + y = 3$

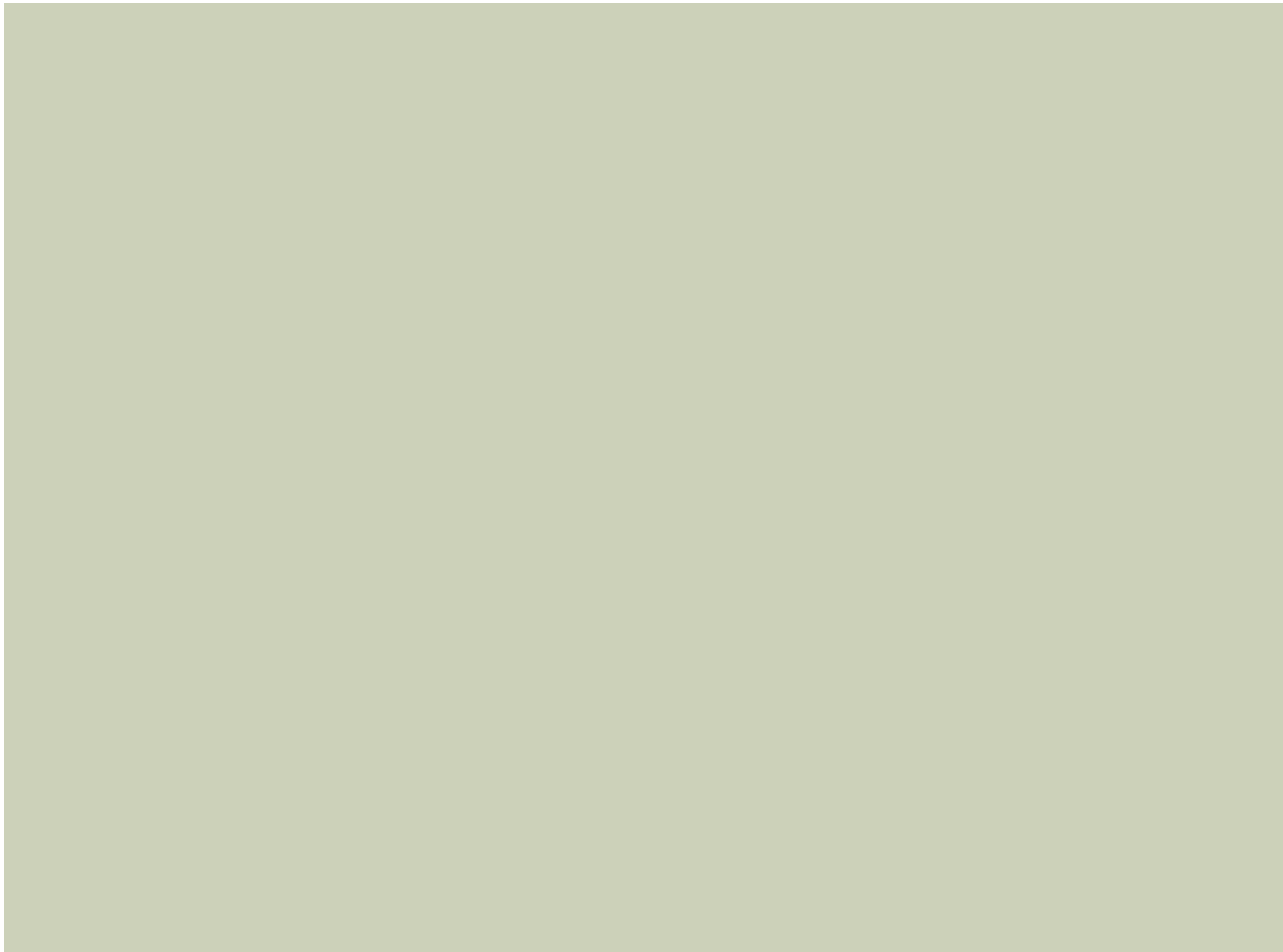




■  $2x + y = -3$

■  $-6x + 3y = 3$







6.2

**SOLVE LINEAR SYSTEMS  
BY SUBSTITUTION**

# METHOD 2: SOLVING BY SUBSTITUTION

- 1) Solve \_\_\_\_\_ of the equations for \_\_\_\_\_  
\_\_\_\_\_.

  - Pick the variable that is \_\_\_\_\_.

- 2) \_\_\_\_\_ the expression from \_\_\_\_\_  
into the \_\_\_\_\_ and \_\_\_\_\_  
\_\_\_\_\_.
- 3) \_\_\_\_\_ the value from \_\_\_\_\_ into  
\_\_\_\_\_ of the equations and \_\_\_\_\_  
for the \_\_\_\_\_.

# NOTEBOOK EXAMPLE #1: SOLVE USING SUBSTITUTION.

- $y = 2x + 5$

- $3x + y = 10$

- $3x + y = -7$

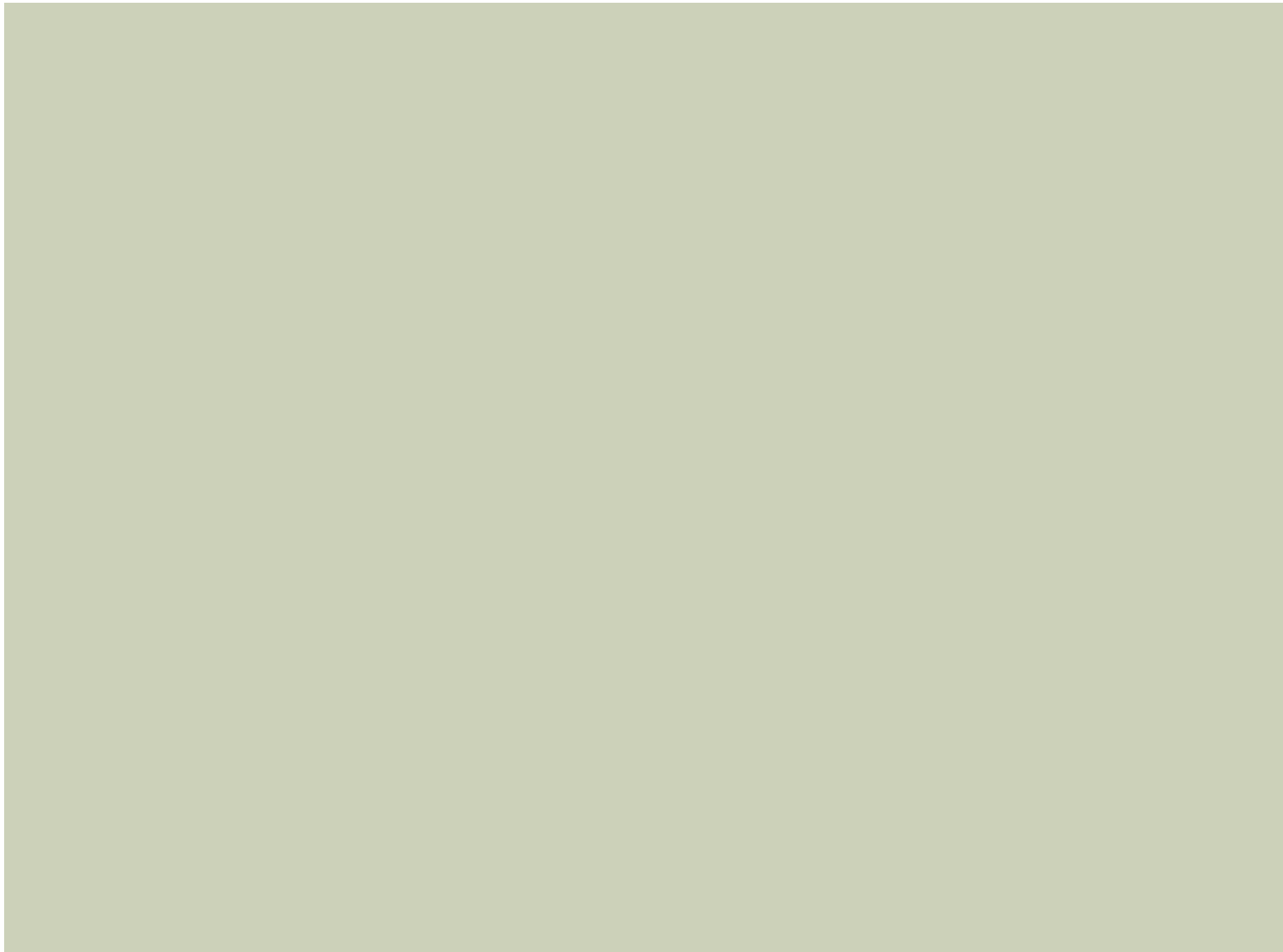
- $-2x + 4y = 0$

- $x + \frac{1}{3}y = -2$

- $-8x - \frac{2}{3}y = 4$

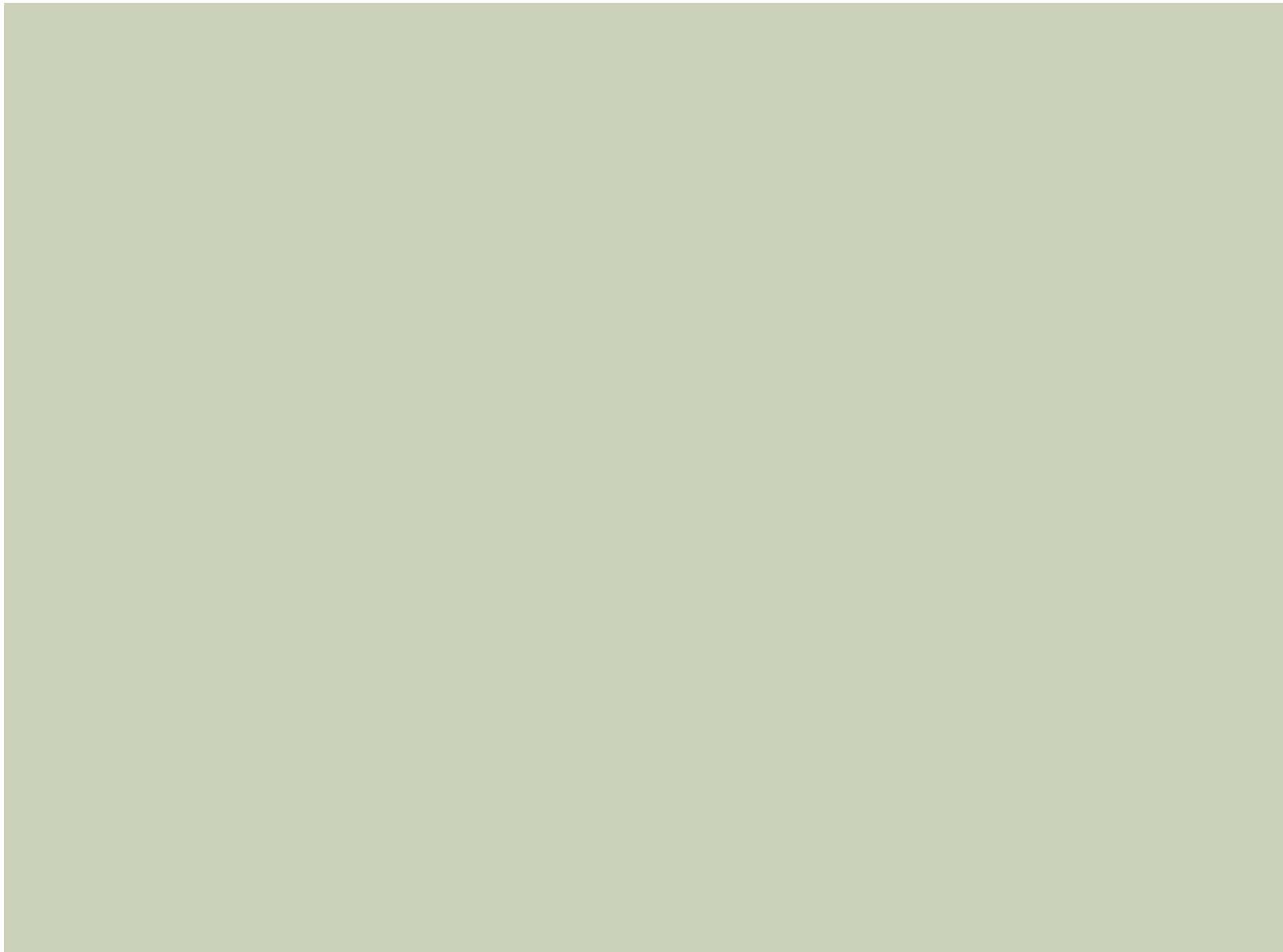
## EX:

- Kara spends \$16 on tubes of paint and disposable brushes for an art project. Each tube of paint costs \$3 and each disposable brush costs \$0.50. Kara purchases twice as many brushes as tubes of paint. Find the number of each that she bought.



## EX:

- A chemist needs 15 liters of a 60% alcohol solution. The chemist has a solution that is 50% alcohol. How many liters of the 50% alcohol solution and pure alcohol should the chemist mix together to make 15 liters of a 60% alcohol solution?



6.3

**SOLVE LINEAR SYSTEMS  
BY ADDING OR  
SUBTRACTING**



# METHOD 3: SOLVING BY ELIMINATION

- 1) \_\_\_\_\_ the equations to \_\_\_\_\_ one variable.
  - Make sure \_\_\_\_\_ are \_\_\_\_\_.
  
- 2) Solve the \_\_\_\_\_ for the \_\_\_\_\_ variable.
  
- 3) \_\_\_\_\_ the value from \_\_\_\_\_ into \_\_\_\_\_ and \_\_\_\_\_ for the \_\_\_\_\_.

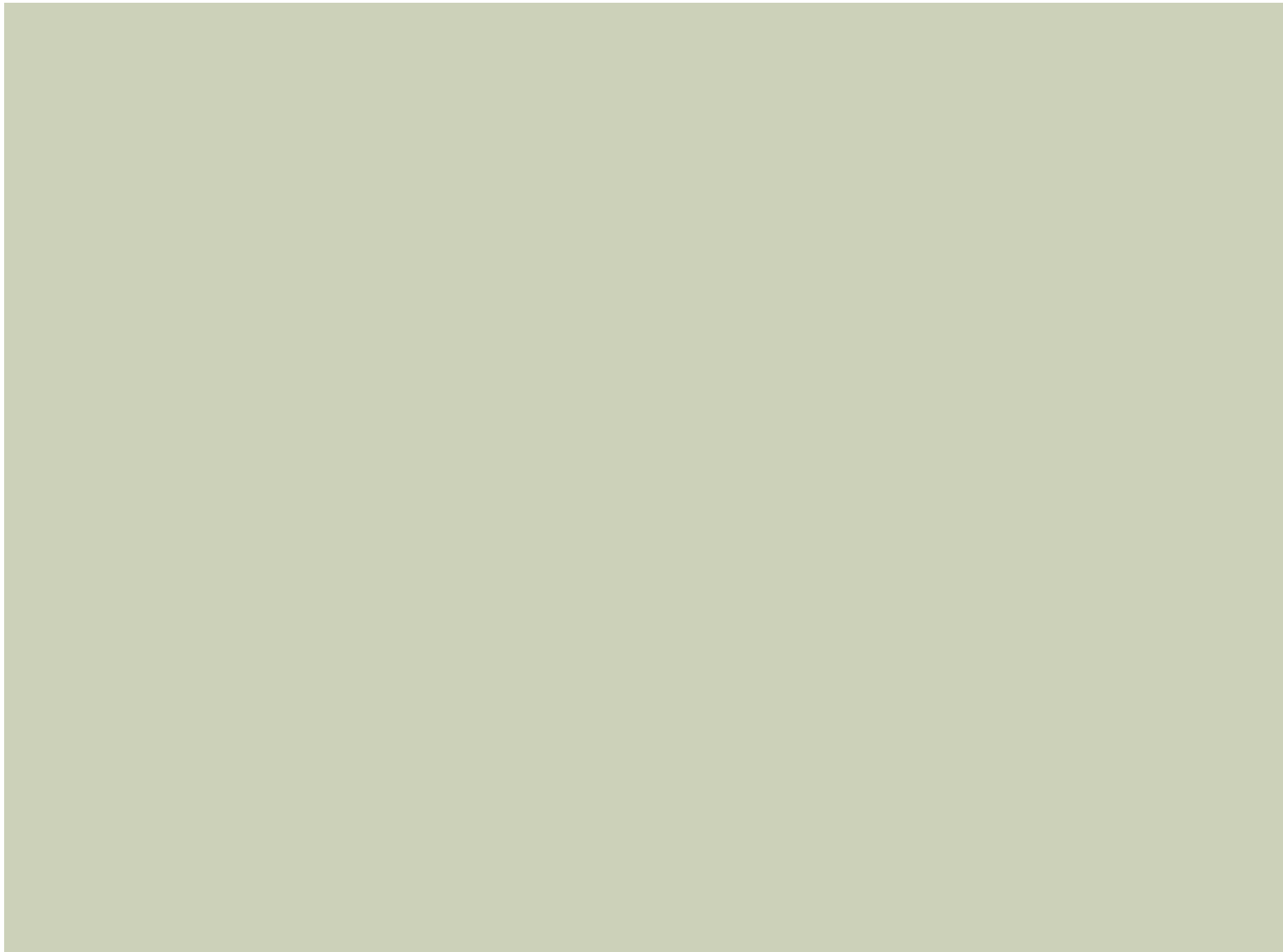
# NOTEBOOK EXAMPLE #2: SOLVE BY ELIMINATION

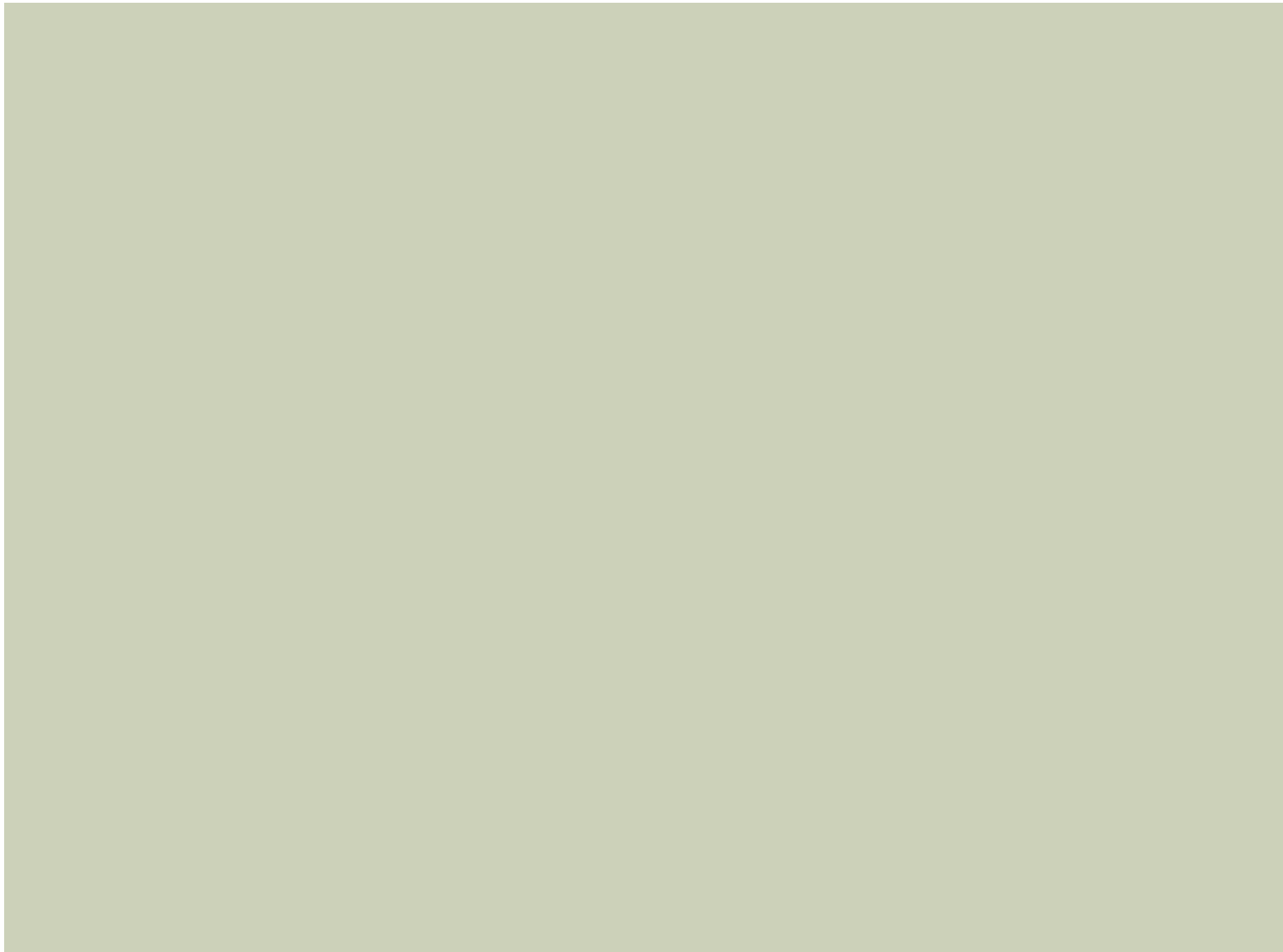
- $4x - 3y = 5$
- $-2x + 3y = -7$
  
- $7x - 2y = 5$
- $7x - 3y = 4$
  
- $3x + 4y = -6$
- $2y = 3x + 6$

# EX:

- During a kayak trip, a kayaker travels 12 miles upstream (against the current) in 3 hours and 12 miles downstream (with the current) in 2 hours. The speed of the kayak remained constant throughout the trip. Find the speed of the kayak in still water and the speed of the current.

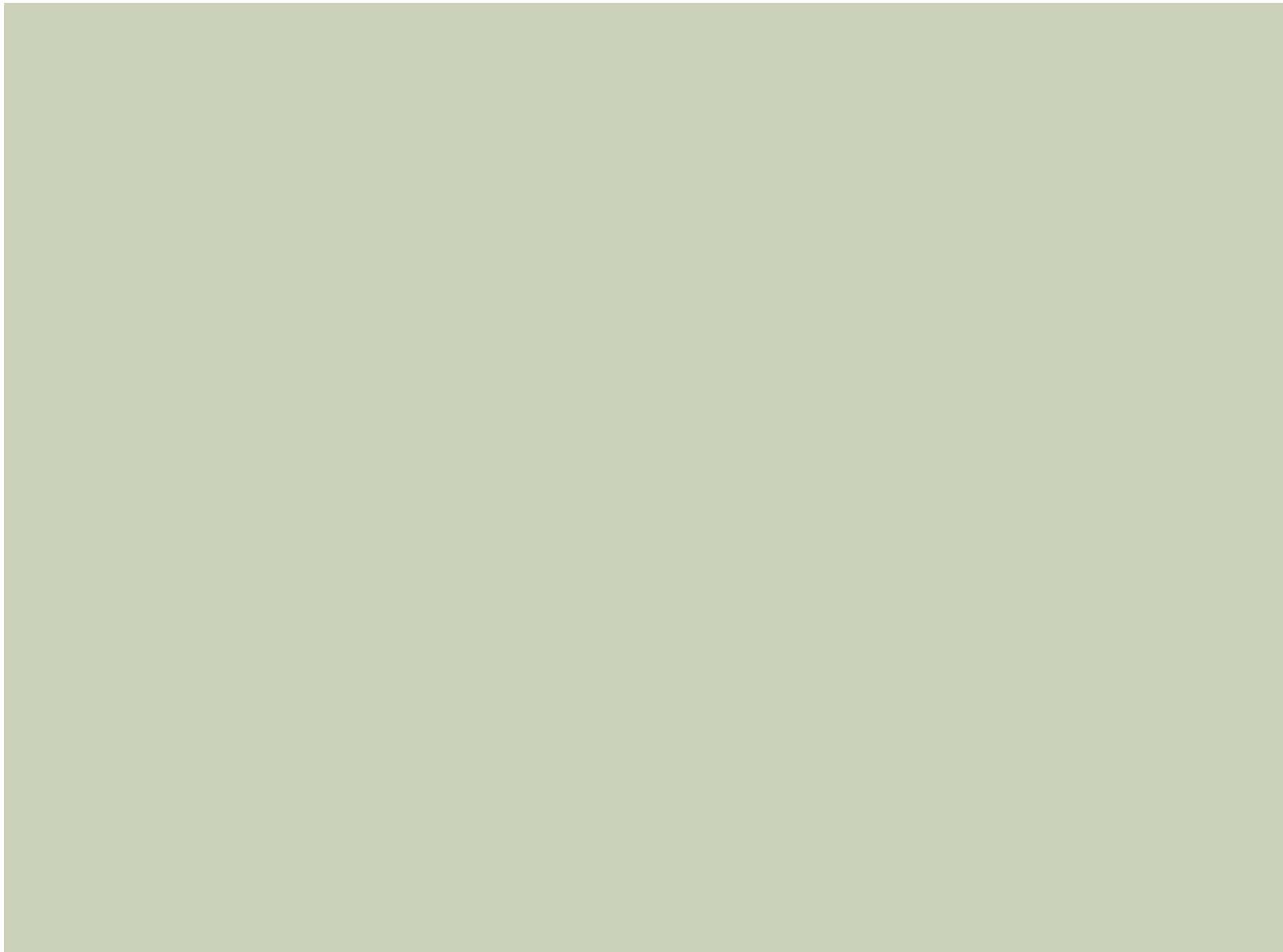
<http://www.physicsclassroom.com/mmedia/vectors/plane.cfm>  
Riverboat Simulator





# EX:

- A business center charges a flat fee to send faxes plus a fee per page. You send one fax with 4 pages for \$5.36 and another fax with 7 pages for \$7.88. Find the flat fee and the cost per page.



6.4

**SOLVE LINEAR SYSTEMS  
BY MULTIPLYING FIRST**



# METHOD 3: SOLVING BY ELIMINATION

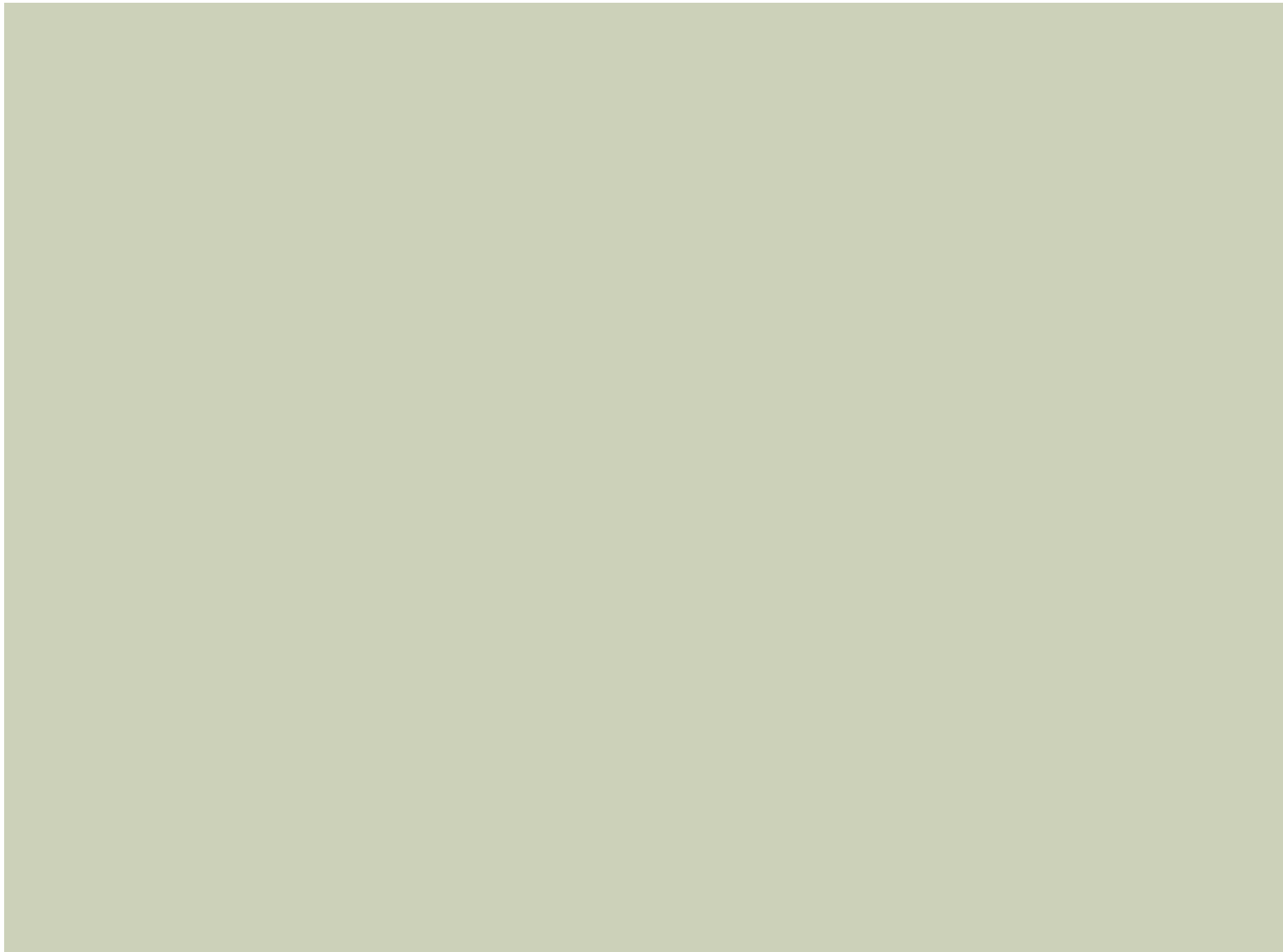
- Sometimes you may have to \_\_\_\_\_ one or both equations by a \_\_\_\_\_ to create \_\_\_\_\_ that are \_\_\_\_\_ of each other.
- Doing this will allow you to \_\_\_\_\_ a variable when the equations are \_\_\_\_\_.

# NOTEBOOK EXAMPLE #3: SOLVE BY ELIMINATION

- $2x + 5y = 3$
- $3x + 10y = -3$
  
- $8x - 5y = 11$
- $4x - 3y = 5$
  
- $3x - 7y = 5$
- $9y = 5x + 5$

## EX:

- Dunham's is having a sale on soccer balls. A soccer coach purchases 10 soccer balls and 2 soccer ball bags for \$155. Another coach purchases 12 soccer balls and 3 soccer ball bags for \$189. Find the cost of a soccer ball and the cost of a soccer ball bag.



6.5

**SOLVE SPECIAL TYPES  
OF LINEAR SYSTEMS**

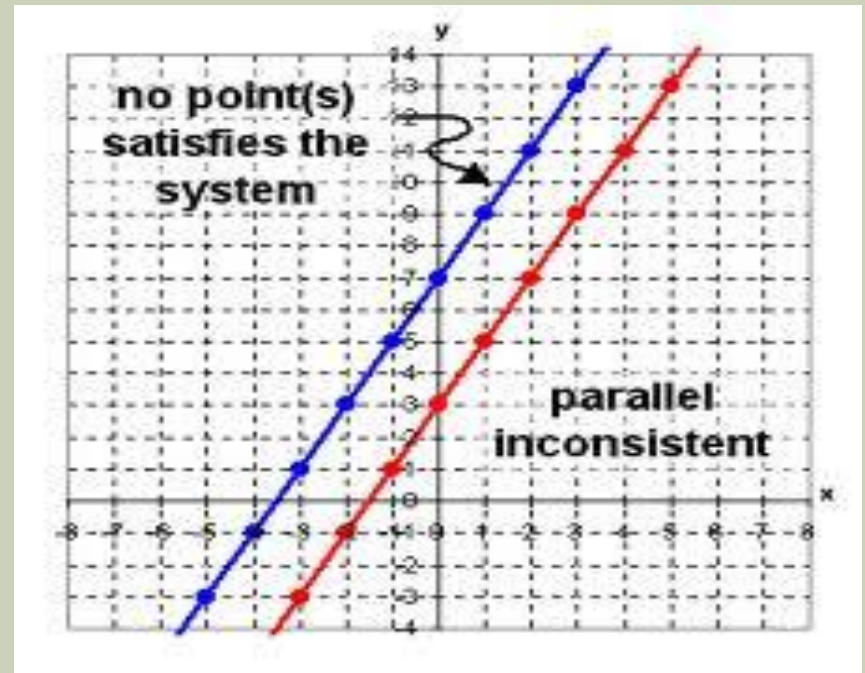
■ A system of equations has \_\_\_\_\_ if the lines are \_\_\_\_\_.

■ Same \_\_\_\_\_.

■ Different \_\_\_\_\_.

■ Called an \_\_\_\_\_.

\_\_\_\_\_.



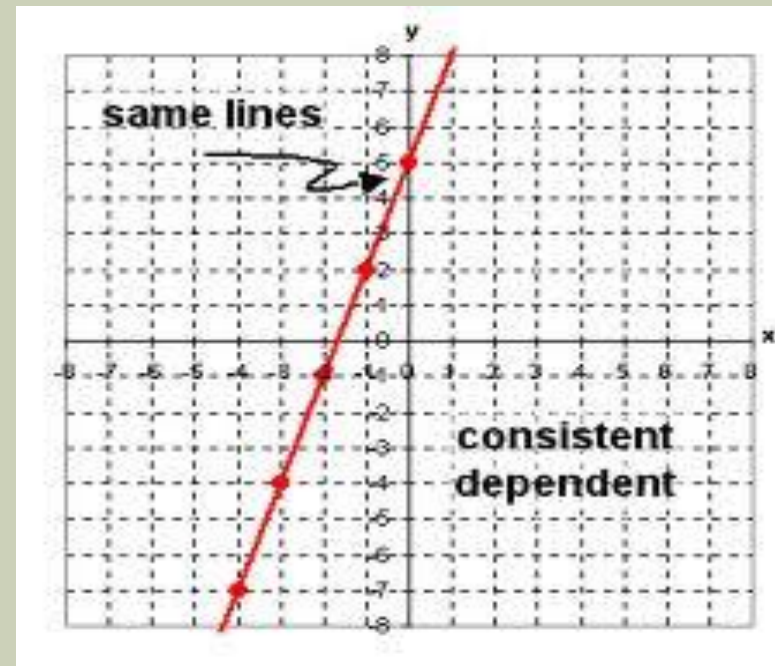
■ A system of equations has \_\_\_\_\_ solutions if the lines are \_\_\_\_\_.

■ Same \_\_\_\_\_.

■ Same \_\_\_\_\_.

■ Called a \_\_\_\_\_

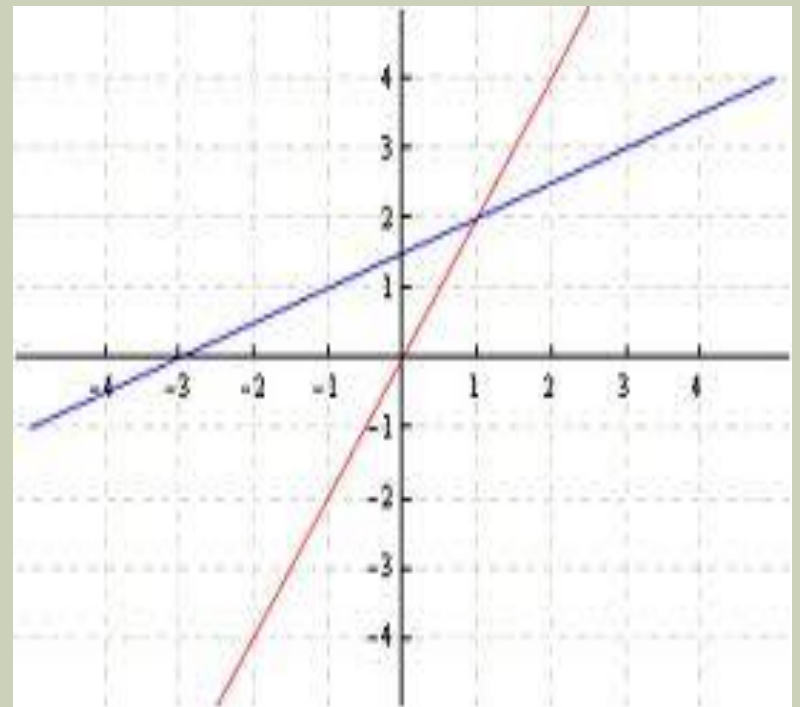
\_\_\_\_\_



■ A system of equations has \_\_\_\_\_ if the lines \_\_\_\_\_.

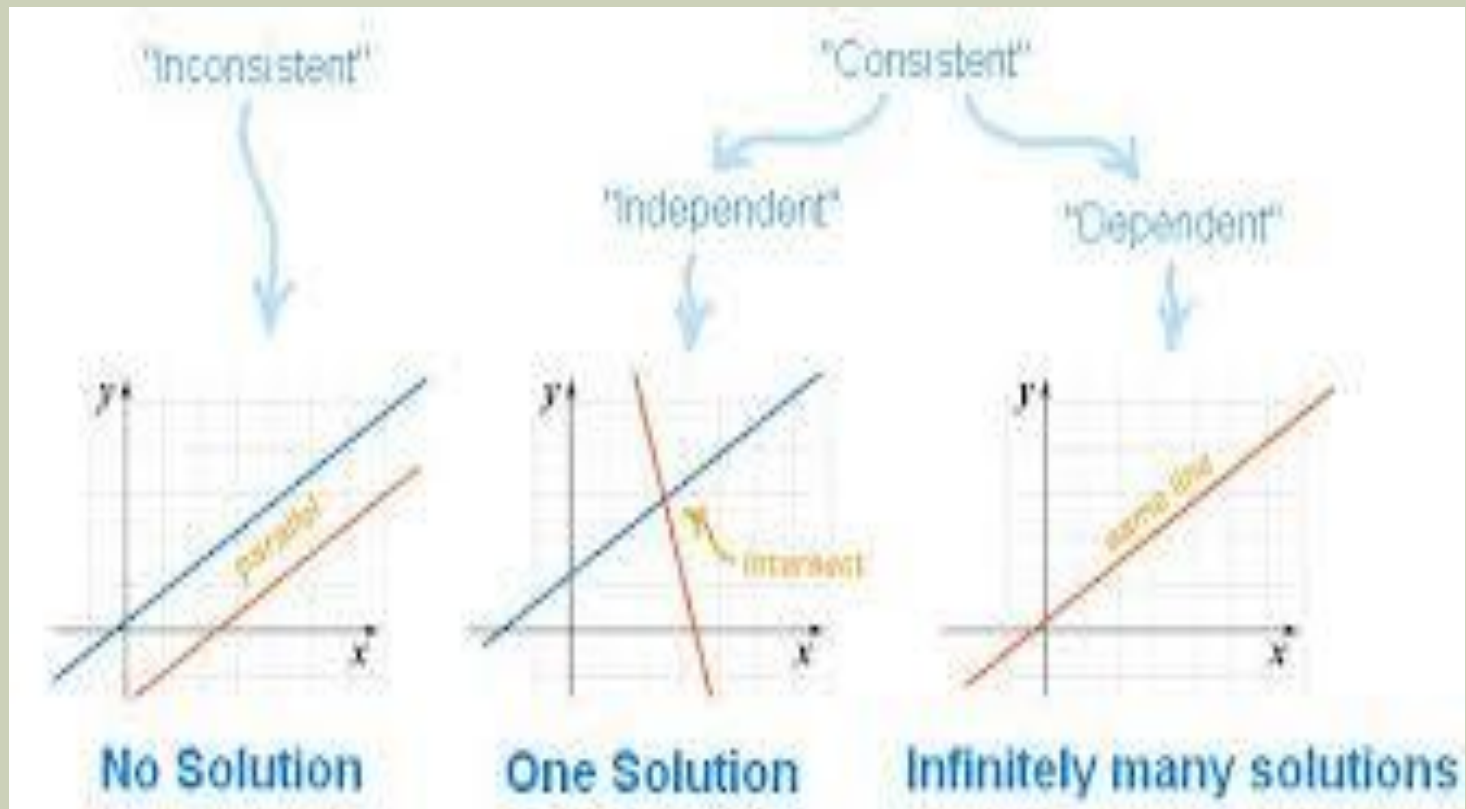
■ Different \_\_\_\_\_.

■ Called \_\_\_\_\_  
\_\_\_\_\_





# SUMMARY:



# NOTEBOOK EXAMPLE #4

## SOLVE THE SYSTEM USING SUBSTITUTION OR ELIMINATION.

- $5x + 3y = 6$

- $15x + 9y = 8$

- $y = 2x - 4$

- $-6x + 3y = -12$

- $3x - 2y = -5$

- $4x + 5y = 47$

# NOTEBOOK EXAMPLE #5

- Without solving the linear system, tell whether it has one solution, no solution, or infinitely many solutions.

- $5x + y = -2$

- $-10x - 2y = 4$

- $6x + 2y = 3$

- $6x + 2y = -5$

# EX:

- A pizza parlor fills two pizza orders. Is there enough information to determine the cost of one medium pizza?

Medium	Large	Cost
4	12	\$168
8	24	\$336

